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Electric field induced instabilities at liquid/liquid interfaces

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External electric fields were used to amplify thermal fluctuations at the interface between two thin liquid films. Similar to the results shown previously for the enhancement of fluctuations at the polymer/air interface, interfacial fluctuations having a well-defined wavelength were enhanced with a characteristic growth rate. A simple theoretical framework to describe the experimental observations is presented. Both experiment and model calculation show a substantial reduction in feature size as a result of the change in surface/interfacial energy when going from the thin film to the bilayer case. Experimentally, features develop nearly 50 times faster for the bilayers in comparison to the polymer/air case. These results point to a simple route by which the nanoscopic feature can be easily and rapidly produced or replicated. © 2001 American Institute of Physics.

INTRODUCTION

Reorganization processes of liquids at interfaces have been studied extensively. The dynamic instabilities of thin liquid films induced by long range van der Waals interactions, i.e., spinodal dewetting, for example, have been the subject of many studies theoretically and experimentally. Spinodal dewetting is characterized by the development of correlated fluctuations at the surface of a liquid film, ultimately leading to the disruption of the film and dewetting. In commercial applications, where film stability is crucial, this is unwanted. However, a controlled structure formation has potential for numerous applications. Miniaturization of these structures into the nanometer range is a desirable, albeit nontrivial, task.

A method to control structure formation at liquid/air interfaces, where electrostatic forces were used to induce an instability at the liquid/air surface of a thin film, was recently reported by Schäffer et al. Their calculations indicated that the instability exhibits a well-defined lateral wavelength, which follows a power-law dependence as a function of the applied electric field. Experiments investigating thin liquid polymer films mounted between parallel capacitor plates with an air gap showed quantitative agreement between experimental data and predictions. A hexagonal array of cylinders spanning the gap between the two electrodes was found to develop. Similar observations were made by Chou and co-workers, however, under conditions where no external electric field was applied.

Here, the findings of Schäffer et al. are extended to the more general case of a liquid bilayer confined between two solid electrodes. Qualitatively, good agreement is found between the experimental observation and the predictions of the extended theory. More generally, the model calculations show a means by which electrically induced instabilities can be used to tune the size scale of self-assembled morphologies from the micron to the submicron level.

EXPERIMENT

Figure 1 shows the typical sample configuration used in this study. Thin liquid films of polyisoprene (PI) and oligomeric styrene (OS) were spin coated from toluene solutions onto bare and gold-coated silicon wafers, respectively. The film thickness was 140 nm. For some experiments, a small air gap was left above the liquid to form liquid/air bilayers. In the remaining experiments, the air was replaced with a layer of oligomeric dimethylsiloxane (ODMS), thus forming a liquid/liquid bilayer. No solvent was used to deposit the ODMS layer. The overall thickness of the bilayer was nominally 1 μm. Table I summarizes the physical constants of the liquid oligomers and polymers. The interfacial tension of OS/ODMS, OS/PI, and PI/ODMS are 6.1, 1.68, and 3.2 mN/m, respectively. The last value was estimated from the segmental interaction parameters χ of different polymer pairs, which follow the order χ_{PS/ODMS} > χ_{PDMS} > χ_{PS/PS}. Thin rails of silicon oxide were evaporated on top of indium–tin–oxide (ITO)-coated microscope slides (Delta Technologies), and these slides were mounted on top of the bilayer samples with the ITO and silicon oxide side facing downward, as shown in Fig. 1. The separation dis-
The characteristic times for the growth of the cylinders were about one half that observed in the single film experiments. A visual comparison of Figs. 2 a and 2 b shows that the time and size scales of the evolving structures was investigated in the second set of experiments. Figure 2 a shows a typical image of this morphology can be seen in Fig. 2 a. The average distance between the center of two neighboring columns is \( d_{\text{cyl-cyl}} \approx 47.4 \pm 4.4 \mu m \).

The influence of changes in \( \epsilon \) and \( \gamma \) of the upper layer on the time and size scales of the evolving structures was investigated in the second set of experiments. Figure 2 b shows the final state of a PI/ODMS bilayer annealed at ambient conditions. A visual comparison of Figs. 2 a and 2 b shows a clear reduction in length scale, associated with the replacement of air by ODMS. The cylinder structures now exhibit a typical spacing of \( d_{\text{cyl-cyl}} = 20.6 \pm 1.3 \mu m \). This spacing is about one half that observed in the single film experiments. The characteristic times for the growth of the cylinders were determined for both the single and bilayers cases by optical microscopic observations. The time required to produce the first observable features was taken as the characteristic time. It is important to note that the time required to produce the cylindrical structures at the PI/ODMS interface was about 1 h, nearly 50 times faster than the time needed to produce the columns in the single film case. Additional experiments on OS/air and OS/ODMS bilayers showed essentially the same behavior, with \( d_{\text{cyl-cyl}} = 12.7 \pm 2.8 \mu m \) for OS/air and \( d_{\text{cyl-cyl}} = 7.6 \pm 2.9 \mu m \) of OS/ODMS.

**DISCUSSION**

The central finding of the experiments presented is a reduction of the length scale of dynamical instabilities induced by an electric field when the liquid/air interface is replaced by a liquid/liquid interface. A reasonable starting point for the discussion of the dynamical instability is the pressure distribution along the interface itself. Similarly to the case of a thin liquid film mounted between parallel capacitor plates leaving an air gap, following previous work, the overall pressure at the interface can be written as

\[
p_2 = p_1 - \gamma_{12} \frac{\partial^2 \Delta h}{\partial \Delta h^2} + p_e(\Delta h) + p_{\text{dis}}(\Delta h),
\]

where \( p_1 \) is the pressure in medium 1 having thickness \( h_1 \); the second term is the Laplace pressure, arising from changes in

<table>
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<th>TABLE I. The physical constants of liquid oligomers and polymer.</th>
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<td>( \gamma ) (mN/m)</td>
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| \( \eta \) (poise)     | 15  
|                        | 400     | 0.1     |
interfacial energy contribution due to changes in the interfacial area. \( \Delta h \) is the local displacement of interface position, \( p_{e} \) is the electrostatic pressure, and \( p_{d} \) is the disjoining pressure. Since \( h_{1} \) and \( h_{2} \) are large in these studies, \( p_{d} \) is negligible in comparison to \( p_{e} \) and the Laplace pressure and, therefore, will be neglected.  

To evaluate Eq. (1) let the origin of the coordinate system be located at the interface between the liquid layers, such that at \( t = 0 \) the interface is located \( z = 0 \). The system is bounded at \( z = h_{1} \) and \( z = h_{2} (h_{2} < 0) \). Local changes in the thickness of the layers are given by \( \Delta h = h_{1} - \Delta h \) and \( \Delta h = h_{2} - \Delta h \). Therefore, the electric field is given by

\[
E_{i} = \frac{\epsilon_{i} U}{\epsilon_{i} \Delta h_{2} + \epsilon_{2} \Delta h_{1}} \quad (i, j = 1, 2; i \neq j),
\]

where \( U \) is the applied voltage and \( \epsilon_{i} \) is the dielectric constant of medium \( i \). For the initial stage of the instability, when the wavelength of the instability \( \lambda \) is much larger than \( \Delta h \), the electrostatic pressure is

\[
p_{d} = -\epsilon_{0} (\epsilon_{2} - \epsilon_{1}) E_{1} E_{2},
\]

where \( \epsilon_{0} \) is the permittivity in a vacuum. It should be noted that this scalar approximation of the electrostatic pressure holds only for the early stages of fluctuation growth, as treated within the framework of the linear instability analysis.

Similar to the model calculations of Vrij, 25 Brochard et al. 3,4 and Schäffer et al., 12,13 a linear stability analysis, which assumes small height fluctuations at the liquid/liquid interface of the form \( \Delta h(x, t) = B e^{i q x} e^{-i \omega t} \), will yield the fastest growing mode of waves in the system. Here, \( q \) is the wave number, \( \tau^{-1} \) is the growth rate, and \( B \) is the amplitude. The modulation of the interface gives rise to a pressure gradient, which induces a lateral flow \( J \) of material. The detailed flow behavior of the coupled system depends strongly on the ratio of the viscosities of the two liquids: \( \eta_{1} \) and \( \eta_{2} \). 22,26 The flux \( J \) can be readily obtained from \( J_{i} = \int_{\Delta h}^{h_{1}} \nu_{x,i} dz \) and \( J_{2} = \int_{h_{2}}^{\Delta h} \nu_{x,2} dz \) using the boundary conditions

\[
\nu_{x,i}(z = h_{2}) = 0, \quad \nu_{x,i}(z = h_{1}) = 0, \quad \nu_{x,1}(z = 0) = \nu_{x,2}(z = 0)
\]

and

\[
\eta_{1} \frac{d \nu_{x,1}}{dz} = \eta_{2} \frac{d \nu_{x,2}}{dz},
\]

where \( \nu_{x,i} \) is the lateral fluid velocity in medium \( i \). This yields

\[
J_{i} = \frac{h_{1}^{2}}{12 \eta_{1} (\eta_{1} \Delta h_{2} + \eta_{2} \Delta h_{1})} \left[ \eta_{2} \Delta h_{1}^{2} - \frac{\partial p_{1}}{\partial x} - 4 \eta_{1} \Delta h_{1} \Delta h_{j} \right] \left[ \frac{\partial \nu_{1}}{\partial x} + 3 \eta_{1} \Delta h_{1}^{2} - \frac{\partial \nu_{2}}{\partial x} \right] (i, j = 1, 2; i \neq j).
\]

Assuming two incompressible liquids coupled by the continuity equations

\[
\frac{\partial J_{1}}{\partial x} + \frac{\partial J_{2}}{\partial x} = 0,
\]

which show the relationship of flow within the two layers, a differential equation describing the dynamic response of the interface is obtained. In the linear approximation, the dispersion relation

\[
\frac{1}{\tau} = \frac{(-h_{1} h_{2})^{3/2}}{5 \eta \gamma_{12} q^{4}} + \frac{\partial p_{e}}{\partial \Delta h}.
\]

is found where \( C(\eta) \) contains all terms involving viscosity, and is given by

\[
C(\eta) = \frac{\gamma_{12}^{2} h_{4}^{2} - \gamma_{12} \eta_{1} \eta_{2} h_{1} h_{2} (4 h_{1}^{2} - 6 h_{1} h_{2} + 4 h_{2}^{2}) + \eta_{2}^{2} h_{1}^{4}}{(-h_{1} h_{2})^{3/2} (\eta_{1} h_{1} - \eta_{2} h_{2})}.
\]

The fastest growing wave number, corresponding to the maximum in Eq. (6), is given by

\[
q_{\text{max}}^{2} = \frac{\epsilon_{0} (\epsilon_{2} - \epsilon_{1})^{2}}{\gamma_{12} U (\epsilon_{1} \epsilon_{2})^{3/2}} (E_{1} E_{2})^{3/2}.
\]

The fastest growing wavelength is found from

\[
\lambda_{\text{max}} = 2 \pi / q_{\text{max}} = 2 \pi \sqrt{\frac{\gamma_{12} U (\epsilon_{1} \epsilon_{2})^{3/2}}{\epsilon_{0} (\epsilon_{2} - \epsilon_{1})^{2}} (E_{1} E_{2})^{-3/4}}.
\]

The characteristic response time \( \tau_{\text{max}} \) is then given by

\[
\tau_{\text{max}} = \frac{3 C(\eta) \gamma_{12} U^{2} \epsilon_{1} \epsilon_{2}}{(-h_{1} h_{2})^{3/2} \epsilon_{0} (\epsilon_{2} - \epsilon_{1})^{4} (E_{1} E_{2})^{3}}.
\]

Consequently, \( \tau_{\text{max}} \) is proportional to \( \gamma_{12} \) as would be expected. 27 If we wish to compare the liquid–liquid case to the liquid–air case presented previously, 12,13 Eq. (9) can be rewritten in terms of the fastest growing wave number defined in Eq. (8a). By substitution we get

\[
\tau_{\text{max}} = \frac{3 C(\eta) \gamma_{12}}{(-h_{1} h_{2})^{3/2} q_{\text{max}}^{4}}.
\]

In the limit of \( \eta_{1} \ll \eta_{2} \), the instability is dominated by the medium with the higher viscosity. In the case where \( \eta_{1} = 0 \), \( \epsilon_{1} = 1 \), and \( \gamma_{12} = \gamma \) (the surface tension of component 2), the equations reduce to the polymer/air case previously described by Schäffer et al. 12,13 The model calculations presented describe only one specific case (comparable to the experimental conditions) but it should be noted that other, more general, theoretical developments have been published by others 20,28,29 that include cylindrical bilayer configurations, gravity contributions, convection effects, and interfacial charge effects.

A comparison of experimental results to theoretical values calculated from Eq. (8b) shows qualitatively good agreement. The model calculations yield \( \lambda_{\text{max}} = 32.47 \mu m \) for the PI/air interface and 17.27 \( \mu m \) for the PI/ODMS interface, which can be compared to the experimental values of 47.4 and 20.6 \( \mu m \), respectively. While experimental values are slightly higher than those predicted, both theory and experiment show a reduction of the length scale by roughly a factor of 2. Also, for the OS/air and OS/ODMS experiments, the
and 7.6 m
regates to the liquid/liquid interface.30–32 Similarly one can
addition of a small amount of a diblock copolymer that seg-
function of the interface or surface tension. It is seen that
Studies are underway to determine the minimum achievable
single layer by placing a surfactant at the liquid/air interface.
achieve an effective reduction of the surface tension of a
liquid/liquid interface. By increasing the difference between
the liquids, i.e., \( \gamma_{12} \), then \( \lambda_{\text{max}} \) reduces to the result shown by Schäffer
et al.\(^{12,13} \) for a thin film with air. In the opposite extreme, \( r = 1 \), i.e., \( \eta_1 = \eta_2 = \gamma_{12} \), representing an
effective eightfold increase in the viscosity. Consequently, \( \lambda_{\text{max}} \) would decrease by a small amount and \( \tau_{\text{max}} \) should increase by a factor of 8. The observation of the 50-fold
reduction in the characteristic time is in disagreement with
this, as seen just by looking at Eq. (9). If we compare insta-
bilities with the same \( q \) vector, in going from the single layer
to the bilayer case, \( C(\gamma) \) increases and \( \gamma_{12} \) decreases. From
Eq. (10) it is seen that this should lead to an increase of \( \tau_{\text{max}} \).
For the case of (PI/ODMS), \( C(\gamma) \) is increased by a factor of
1.01 and \( \gamma_{12} \) decreases by a factor of 10, yielding a com-
bined increase in \( \tau \) of 14. Now, \( q \) increases by a factor of 1.9 or \( q^d \) increases by a factor of 13.0. Together, these factors
should cancel each other, meaning that the growth rate of the
instabilities in the PI single layer and in the PI/PDMS double
layers is approximately the same (\( \tau_{\text{max}} = 0.27 \text{ h for the PI/air} \)
case and \( \tau_{\text{max}} = 0.22 \text{ h for the PI/ODMS case} \)). However, the
the time at which features are observed in the bilayers case is
nearly 50 times shorter than that seen in the single layer case.
The exact origin of this discrepancy is not known at present.
However, the arguments presented here are valid only for the
early stages of growth. Late stage processes, which govern
the formation of columns (the experimental observable), re-
quire a much more detailed analysis.

CONCLUSIONS

We have extended earlier studies of field-induced struc-
ture formation in single layer liquid films to include the more
general case of a bilayer. Initial experiments show, consistent
with an extended model, a reduction of the characteristic
length scale of fluctuations at the liquid/liquid interface.
However, a marked decrease in the time constant was found
in contrast to the simple model. Calculations indicate that a
further decrease in the size scale is possible by a reduction of
interfacial tension between the two media.

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(T.K.).

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We independently determined the resistivity of the ITO layer \( (R_{\text{ITO}} = 320 \, \Omega) \) and the resistivity of the highly doped Si wafers \( (R_{\text{Si}} = 0.01 - 0.03 \, \Omega/cm) \). Considering the typical currents measured during the experiment \( I \sim 5 \, \mu A \) this indicates that the applied potential indeed dropped over the sample capacitor.
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