

# Gauss Introduction

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## preliminary remarks

### advantages of GAUSS

- GAUSS = software package for statistical and econometric purposes; quasi-standard amongst econometricians; many implemented procedures
- its programming language is easily learned and is very similar to MATLAB
- central data element is the matrix, i.e. formulae can be entered intuitively

## disadvantages

- no public domain software; expensive
- relatively few books/ scarce documentation →  
**Use** the very good User's Guide and Reference help files!!!

## user interface

- input can either be entered directly in the command input-output window → command will be executed directly or in the editor window  
→ complete code file will be executed by clicking on the run button
- the error output-window will become handy...

## Writing a program

- programs can be written in any editor as ASCII-files; use of GAUSS editor recommended, though
- program files can have any file extension, sensible choice: .prg
- you can define a working directory on the tool-bar. GAUSS will look for your files there

## GAUSS basics

- GAUSS is *not* case-sensitive!
- some variable names are forbidden as they refer to internal procedures, e.g. abs, and, cls
- **Use** comments!!! @ comment @ or /\* comment \*/ or ‘comment’ if the comment should be printed in the output window
- cls clears the input-output window
- new clears the memory

## Generating matrices and matrix manipulation

- variables are defined 'on the go', i.e.  $a=5$   
 → scalars and variables are just special matrices
- matrices are defined row by row, i.e.  $A=\{1\ 2, 3\ 4\}$  generates

$$\mathbf{A} = \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix}; \mathbf{B} = \begin{pmatrix} 5 & 6 \\ 7 & 8 \end{pmatrix}$$

$\mathbf{B}$  is generated accordingly



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- individual elements  $e_{ij}$  of a matrix can be addressed by `newvarname=varname[i,j]` where  $i$  and  $j$  are the row and column position  
*example:* 3 is the  $e_{21}$  element of  $\mathbf{A}$  and can be extracted by `newvarname=varname[2,1]`
- whole columns can be addressed by `varname[.,1]`
- **WARNING:** GAUSS overwrites preexisting variables without a prior warning or error message!!!
- sometimes, it is useful to generate an empty matrix by `u={}`

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- horizontal concatenation of two matrices:  $a \sim b$ ; vertical concatenation by  $a | b$

*example:*  $c = a \sim b$  returns

$$C = \begin{pmatrix} 1 & 2 & 5 & 6 \\ 3 & 4 & 7 & 8 \end{pmatrix}$$

$d = a | b$  returns

$$D = \begin{pmatrix} 1 & 2 \\ 3 & 4 \\ 5 & 6 \\ 7 & 8 \end{pmatrix}$$



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- `cols(varname)` and `rows(varname)` returns the number of columns and rows of a matrix  
*example:* `cols(C)` returns 4; `rows(C)` returns 2
- Hint: Always make sure that you know the dimension of the output of GAUSS procedures. Is the result of a row or a column vector?

## Operators, matrix algebra

### operators for scalars

- all basic mathematical operators like  $+$ ,  $-$ ,  $*$ ,  $/$  can be used
- variables can be raised to power  $n$  by  $\wedge n$ , faculty uses !
- basic calculus rules known from algebra apply

### relational operators

$==$  (eq);  $\neq$  (ne);  $>$  (gt);  
 $<$  (lt);  $\geq$  (ge);  $\leq$  (le);



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- The result of a logical operation of the form  $t = a \text{ op } b$  (where  $\text{op}$  is one of the aforementioned operators) is a logical variable  $\rightarrow$  false=0 and true=1

### logical operators

and, or and not can also be used

*Create two matrices of the same dimensions. Read out the first row of each matrix and try horizontal and vertical concatenation. Write comments into your program. Try the commands: cols, rows, cls, new. Create two scalars and try out the relational operators given above.*

## Matrix algebra

- standard matrix algebra calculus rules apply
- $\mathbf{A}'$  yields the transpose of  $\mathbf{A}$

$$\mathbf{A}' = \begin{pmatrix} 1 & 3 \\ 2 & 4 \end{pmatrix}$$

- element-wise operations: adding and subtracting matrices by  $+$ ,  $-$ , multiplying and dividing a matrix by a scalar  $*$ ,  $/$
- Remember: Matrix multiplication and inversion of matrices is not an element-wise operation!  
`inv(matname)` and `*` follow laws of matrix calculus

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- elementwise operations are possible! `a.*b` yields

$$\begin{pmatrix} a_{11} \cdot b_{11} & a_{12} \cdot b_{12} \\ a_{21} \cdot b_{21} & a_{22} \cdot b_{22} \end{pmatrix} = \begin{pmatrix} 1 \cdot 5 & 2 \cdot 6 \\ 3 \cdot 7 & 4 \cdot 8 \end{pmatrix}$$

- further element-wise operators are `./` and `.^`
- Matrices can also be multiplied element-wise by a vector
- All *logical* and *relational* operators can also be applied element-wise:  
`.op`

## further matrix commands

### further commands for generating special matrices

- `seqa(start,incr,times)`
- `ones(rows,cols)`, `zeros(rows,cols)`, `eye(dim)`

### further matrix functions

- `sumc(matname)`, `cumsumc(matname)`
- `selif(matname,e)`, `delif(matname,e)`

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- `diag(matname)`
- `rank(matname)`, `det(matname)`, `eig(matname)`

*Create a  $2 \times 2$  matrix that has fours on its diagonal and a  $2 \times 2$  matrix of ones. Try matrix multiplication as well as elementwise multiplication. Try the commands `diag`, `sumc` ect.*

## Procedures

- efficient way of programming
- procedures are used to repeat program code with different arguments
- the difference between local and global variables is important. Local variables are only used within the procedure. Global variables are used everywhere in the program.



## Syntax of a Procedure

```
proc(number of outputarguments) = procname(inputarg1,inputarg2,...);  
local locavar1,locavar2,locavar3...;  
< body operations >;  
retp(outputarg1,outputarg2,...);  
endp;
```

call the procedure:

```
{outputarg1,outputarg2,...} = procname(inputarguments);
```

*Exercise: Write a procedure that multiplies two matrices  $X$  and  $Y$ . Call the procedure.*



## if-else-elseif-endif...conditional branching

```
if condition1;  
< do this 1 >;  
elseif condition2;  
< do this 2 >;  
...  
else;  
< do this 3 >;  
endif;
```

The else and elseif statements are optional.

*Exercise: Use the matrix multiplication procedure from above and check for conformity of the matrices in the procedures. If they do not conform print out a comment and stop the program.*

## while, and until, for...loop statements

### Syntax of a loop statement: for

```
for i (start, stop, step);  
< do this >;  
endfor;
```

unconditional loop statement

used if the number of repetitions is certain and does not depend on a condition

*Exercise: create a zero matrix of dimension 10 times 4 and write in each row the actual time using a **for** statement. Hint: **time** delivers the actual time.*

## while, and until, for...loop statements

### Syntax of a loop statement: while and until

<code>do while condition;</code>	<code>do until condition;</code>
<code>&lt; do this &gt;;</code>	<code>&lt; do this &gt;;</code>
<code>endo;</code>	<code>endo;</code>

conditional loop statement

`do while` is executed as long as the condition is true

(loop action is skipped as soon the condition is wrong)

`do until` is executed as long as the condition is wrong

(loop action is skipped as soon the condition is true)

syntax for `do until` and `do while` is identical

Exercise: As previous exercise, but use a `do while` and `do until` statement instead.



## while, **and** do until, for...loop statements

Hint: Use vector operations instead of loops if possible.

*Exercise: create a data vector of natural numbers from 1 to 100000. Compute the sum of this rows (a) with a for loop and (b) with a conditional loop and (c) with an inner product. Measure the time difference between the three variants. Hint: Use the function `hsec`.*

## save **and** load... **GAUSS** data format

- there are many different ways to load and save data in GAUSS
- supported formats are e.g.: .asc .txt .xls .fmt .dat ...
- load syntax for .txt or .asc: `load varname[r,c] = filename.txt` or `load varname[] = filename.txt`
- load syntax for .fmt: `load varname = filename.fmt`
- save syntax: `save filename = varname` (GAUSS saves in a fmt format)

*Exercise: Save and load a self-designed matrix as .fmt*

## Statistical Functions in GAUSS

- `meanc(varname)` and `stdc(varname)`
- `median(varname)` and `quantile(varname,probs)`
- `corr(x,varname)`
- `ols()`

*Exercise: use a data matrix and try all statistical functions*

## Graphs in GAUSS

- complex and extensive graphics features possible
- it is recommended to use a more sophisticated graphical software
- "quick and dirty" graphs
- activation of graphics tool by calling the library by the command:  
`library pgraph; graphset;` The second command resets all global variables in the library to the default values.



## Graphics commands in GAUSS

- `xy(x,y)` twodimensional coordinate axes with x and y on x- and y-axis
- `bar(varname,ht)` bar chart
- `hist(varname,bp)` histogram
- `xyz(x,y,z)` three dimensional graphic

## More graphics details

- all global variables in the `pgraph` look like `_p...`
- consider `xy(x,y)`: `_plctrl` controls the lines between the points `x` and `y`  
if `_plctrl=0` (default) the points are connected by lines; if `_plctrl=-1` the points are not connected.
- `_plwidth` controls the line width
- note: the new settings are valid until they are either changed or reset by `graphset`.



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- with the command `window(r,c,t)`, it is possible to combine graphics to one graph `r` and `c` are the number of rows and columns, respectively and `t` the character of the graphic (transparent or not)
- note: There are some graphics examples in `c:\gauss6.0\examples`
- `title(" graph name "); xlabel(" label name ")`

## Probability Distributions

- there are many commands for the computation of distribution functions, inverse distribution function, complement of a distribution function ( $1-F(x)$ ) and probability functions
- example: standard normal probability function  $\text{pdfn}(x)$  with associated distribution function  $\text{cdfn}(x)$ , complement  $\text{cdfnc}(x)$

*Exercise: Plot the density function of a  $N(0,1)$  random number in a graph.*

## Random Numbers

- there are GAUSS commands for the computation of random numbers
- example: standard normal-, uniform-, gamma-, poisson-, negative binomial- random numbers,...
- syntax example for drawing a uniform random number:  $u = \text{rndu}(r,c)$   
r and c are the number of rows and columns

## Exercise: OLS

- Import to Gauss the file `wages1_data.txt` (download from homepage) which contains 3296 observations taken from a US Household Panel. Overview of the imported data: column structure from first to fourth column `exper`: experience in years `male`: 1 if male, 0 otherwise `educ`: years of schooling `wage`: wage (in \$) per hour

- Reproduce the descriptive statistics in the table below.

Variable	Obs	Mean	Std. Dev.	Min	Max
<code>exper</code>	3296	8.041869	2.290855	1	18
<code>male</code>	3296	.5239684	.499501	0	1
<code>educ</code>	3296	11.63016	1.657114	3	16
<code>wage</code>	3296	5.816391	4.054694	.0765556	112.7919

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- Plot the histogram of wage and save the graph.
- Estimate the following regression models by OLS and interpret  $\beta_2$  (the returns of schooling).

a)  $wage_i = \beta_1 + \beta_2 educ_i + \beta_3 exper_i + \varepsilon_i$

b)  $\ln wage_i = \beta_1 + \beta_2 educ_i + \beta_3 exper_i + \varepsilon_i$

Hints: write a OLS procedure that includes the following:

1) Define  $y$  and  $x$ .

2) compute the ols estimator:  $\mathbf{b} = (\mathbf{X}'\mathbf{X})^{-1}\mathbf{X}'\mathbf{y}$

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3) Compute the Variance-Covariance matrix of the OLS estimator:

$$\text{Var}(b) = s^2(X'X)^{-1} \text{ with } s^2 = \sum e_i^2 / (n - k)$$

4) Compute the t-test with  $H_0 : \bar{\beta}_k = 0$   $t_k = \frac{\beta_k - \bar{\beta}_k}{se(b_k)}$

5) Print the output of coefficient, standard error and t-test in the Output window.

- compare your results with the OLS Gauss procedure results