

Definition (Kernel):

Consider a bounded function $K(\cdot)$ such that $\int K(\psi)d\psi = 1$.

Assumption Density Estimation I:

$K(\cdot)$ is a bounded, symmetric around 0 function satisfying:

$$\int K(\psi)d\psi = 1 \quad (1)$$

$$\int \psi^2 K(\psi)d\psi = \mu_2 \neq 0 \quad (2)$$

$$\int K^2(\psi)d\psi = c < \infty \quad (3)$$

Assumption Density Estimation II:

The observations $x_1, \dots, x_i, \dots, x_n$ are iid over i .

Assumption Density Estimation III:

f is three times continuously differentiable with bounded third derivatives.

Assumption Density Estimation IV:

As $n \rightarrow \infty$ and $h \rightarrow 0$, $nh \rightarrow \infty$.

Assumption Density Estimation I':

Let $K(\cdot)$ be a symmetric, continuous, bounded function, such that:

$$\int \psi^k K(\psi)d\psi = \begin{cases} 1 & \text{if } k = 0 \\ 0 & \text{if } k = 1, \dots, r-1 \\ \mu_r < \infty & \text{if } k = r \end{cases} \quad (4)$$

Assumption Density Estimation III':

f is $r+1$ th order continuously differentiable with bounded derivatives.