



**Preparatory Course for
Mathematical Methods in Economics and Business**

2. Exercise Sheet

Exercise 1 (Linear Equations)

Solve the following equations for the unknown x :

(a) $\frac{1}{x-1} = \frac{3}{2x+3}$

(b) $\sqrt{3-x} = 2$

(c) $\sqrt[5]{5-x} = -2$

(d) $(x-6)^{\frac{1}{3}} = 2$

Exercise 2 (Quadratic Equations)

State the solution set \mathbb{L} for the following equations for $x \in \mathbb{R}$:

(a) $x^2 - 10 = 3x$

(b) $3 \frac{x^3 - 5}{x^2 + 5} = 3x - 5$

Exercise 3

Solve the following equations for the indicated variable:

(a) $\alpha x - a = \beta x - b$ for x

(b) $\sqrt{K} \cdot \left(\frac{1}{2} \frac{r}{w} K\right)^{\frac{1}{4}} = Q$ for K

(c) $\frac{1}{s} + \frac{1}{T} = \frac{1}{t}$ for s

(d) $\frac{x-2y+xz}{x-z} = 4y$ for z

Exercise 4 (Inequalities / Intervals)

For which x do the following inequalities hold?

(a) $-3x + 2 < 5$

(b) $\frac{x-1}{x+3} \leq 0$

Exercise 5 (Inequalities / Intervals)

Determine the solution set for the following inequalities:

(a) $\frac{x-2}{4-x} \geq 0$; $x \in \mathbb{R} \setminus \{4\}$

(b) $\frac{3x-1}{2x+1} \leq 3$; $x \in \mathbb{R} \setminus \{-\frac{1}{2}\}$

(c) $\frac{5x^2-1}{x+1} \leq 2x-1$ $x \in \mathbb{R} \setminus \{-1\}$

(d) $|x+1| \leq \frac{1}{2} |x| + 1$; $x \in \mathbb{R}$

Exercise 6 (Absolute Values)

Determine x such that:

(a) $|3-2x| = 5$

(b) $|x-2| \leq 1$

(c) $|x| > \sqrt{2}$

(d) $|x^2-2| \leq 1$