

2010b). I suggested that the invention of the clay-token system offered a “material scaffold” able to objectify and simplify the problem of number and thus to restructure the cognitive task needed for its solution. This restructuring may have forged an extended reorganization in the neural connectivity of the critical intraparietal areas associated with numerosity. In other words, the tangible material reality of the clay token—as an “epistemic” artefact (Kirsh 1995)—made possible that the parietal system, previously evolved to support numerosity, gets reorganized and thus partially “recycled” to support the representation of exact number (cf. Piazza and Izard 2009).

The above hypothesis, I think, is consistent and complementary with much that is being proposed by Coolidge and Overmann, especially in terms of the neurological network of numerosity and the links with metaphorical thinking. Where our views seem to diverge nonetheless is in how we perceive the role of material culture in the development of numerical thinking. The “internalist” foundation of Coolidge and Overmann’s model allows that material culture can only be seen as a passive externalization device. On this construal, the clay token may well facilitate or provide the stimulus for the expression of number, but the mental process that *really matters* is realized in neural tissue and localized somewhere in the parietal regions of the brain. In other words, for Coolidge and Overmann the process responsible for the development of numerical and symbolic thinking takes place inside the head (but see Overmann, Wynn, and Coolidge 2011). I propose instead that this process extends beyond skin and skull and would have been impossible to achieve by the unaided biological brain. In fact, I argue for the ontological priority of material engagement in the emergence of abstract thinking and symbolic number. What this claim holds, put simply, is that the material instantiation of the concept of number must precede or coemerge with its neural instantiation. From such an enactive perspective, finger counting, engraved marks, or clay tokens do more than simply *stand for* number: they *bring forth* the number (Malaouris 2008, 2010a).

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Coolidge and Overmann have gathered an impressive amount of material from disparate areas such as semiotics, developmental psychology, neurobiology, and archaeology. Particularly inspiring are their views about the putative cognitive factors motivating analogical reasoning and metaphoric thinking in us humans. Here, I would like to take a slightly different stance on what it means to understand symbols. Reviewing neurobiological evidence, I will arrive at the conclusion that the PFC, not the parietal cortex, endows *Homo sapiens* with symbolic thinking.

In the target article, the term “symbol” (and thus “symbolic thinking”) is used for all sorts of associations between a signifier and a signified. This is problematic because not all referential associations need to be symbolic. Referential associations can adopt different levels of complexity (Deacon 1997; Peirce 1955), from icons (reference based on similarity) and indexes (reference based on contiguity or correlation) to symbols (arbitrary signs embedded in a referential system). Symbolic reference is crucially a link between sign-sign relations, not between individual sign-object relations. As a consequence, only symbols can be manipulated on the basis of compositional rules (i.e., syntax). When evaluating the emergence of symbolic thinking in *H. sapiens*, this distinction becomes essential because only symbolic reference distinguishes humans from animals. Iconic (tally sticks, finger counting, shell beads) and indexical (shape-quantity associations) representations of cardinality can also be mastered by animals (Diester and Nieder 2007), but such representations do not progress on to the level of symbols. Evidence for iconic stages can be found both in human history and in children’s acquisition of numbers (Wiese 2003). Children, however, rapidly transcend this stage, and numerical competence in humans passes from an iconic to an indexical and finally symbolic stage. This is the striking discontinuity that needs to be explained during human evolution.

Which brain area allows us to establish semantic associations to ultimately arrive at a symbol system? The authors advocate the parietal lobe, and the IPS in particular, as the key structure for the emergence of symbolic thinking. The IPS is surely a core structure for the representation of semantic aspects of numerical quantity (Nieder and Dehaene 2009; Nieder, Diester, and Tudusciuc 2006). However, neurobiological evidence suggests that the (granular) PFC may fulfill the requirements necessary for high-order associations between signs, ultimately giving rise to the cultural invention of linguistic and number symbols (Nieder 2009). This development can be witnessed both phylogenetically (in non-human primates) and ontogenetically (in human infants).

Diester and Nieder (2007) trained rhesus monkeys to associate the shapes of Arabic numerals with the numerosity of dot patterns ranging from 1 to 4. Only in the PFC, but not in the IPS, many of the same neurons were equally active to the numerical values assigned to the numeral shapes. Thus, in nonhuman primates, both prefrontal and parietal neurons represent numerical values, but unlike parietal neurons, only prefrontal neurons have the additional capacity to associate numerosity and an Arabic numeral shape as its indexical referent. These findings suggest the PFC as the prime phylogenetic source in the mapping process of initially meaningless shapes to semantic categories, giving rise to an indexical understanding of signs. Support for this assumption comes from recent fMRI studies with children. When comparing numerical values in symbolic (numerals) and nonsymbolic notation (sets of dots), children at the ages of six and seven invoke the same cortical networks previously described for adults,

with parietal brain regions as key structures. Interestingly, however, children also recruit the inferior frontal cortex (granular frontal cortex BA 44/45) for notation-independent numerical processing to a much greater degree than adults (Cantlon et al. 2009; Kaufmann et al. 2006). Similarly, a greater engagement of frontal brain regions during Arabic numeral judgments (Ansari et al. 2005) and symbolic arithmetic tasks (Rivera et al. 2005) has been described in children compared with adults. These results point to the PFC as the cardinal structure in acquiring a symbolic number concept during ontogeny. Only with age and proficiency, the activation seems to shift to parietal areas.

Coolidge and Overmann concentrate on semantic aspects of symbol systems. However, to establish a full-fledged symbol system, meaningful sign-object associations must be accompanied by rules guiding the structuring of signs (syntax). Syntax and semantics of individual sign-sign relations are inextricably linked. Such circuitry representing rules is also hosted by the PFC. In monkeys required to flexibly switch between “greater than/less than” rules, Bongard and Nieder (2010) have recently shown that the activity of single neurons reflected these abstract numerical rules. We speculate that these neuronal circuits in the monkey lateral PFC could readily have been adopted in the course of primate evolution for syntactic processing of numbers in formalized mathematical systems. The collected empirical evidence argues that the network of the PFC, not the parietal cortex, endowed us humans with full-fledged symbolic thinking.

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Coolidge and Overmann discuss the neurological substrate of numerosity processing because it is one of the a priori conditions for numerosity processing to play a role in the development of the abstraction capacity. In this description they make two inappropriate assumptions that are unfortunately very frequently made, even by researchers in the field. First, they consider the brains of monkeys and humans to be highly similar and presume that anatomical regions such as the IPS correspond functionally in the two species. The human brain is much larger than that of monkeys: the human cortical surface is about 10 times that of monkeys. The two species, which diverged over 23 MYA, exhibit quite different behaviors, and it therefore is not surprising that at least in some respects the brains of the two species differ significantly. One such instance is the inferior parietal cortex, which is greatly expanded in humans (Van Essen and Dierker 2007). As a consequence, human cortical regions corresponding to monkey regions located in the IPS have moved dorsally and are located in the medial wall of the human IPS or even in the adjacent superior parietal lobule (SPL; Durand et al. 2009;

Grefkes and Fink 2005). In the monkey, numerosity-selective neurons are located in the ventral intraparietal area (Nieder and Miller 2004), and their human counterparts should therefore be located in the SPL. The second point of confusion is between recording single neurons and fMRI. The latter technique measures a hemodynamic response in so-called voxels, which are typically a few millimeters on a side and include millions of neurons. Given the pooling of so many neurons, it is difficult for fMRI to quantify the main property of single neurons in that sample: their selectivity for a functional aspect of the stimulus, here numerosity. Indirect techniques, such as repetition suppression or multivoxel analysis, have been devised to circumvent these limitations, but with only limited success (Sawamura, Orban, and Vogels 2006). A meaningful relationship between single neurons recorded in monkeys and fMRI data obtained in humans can, however, be established using monkey fMRI as a linking technique (Orban 2011).

In their discussion concerning the abstraction of numerosity, the authors describe two processes: linking a sensory (e.g., visual) representation of a number of objects to a symbol (the number) and relating ordered sequences of numbers to sequences of other symbolic entities such as days or months. The latter process has a higher chance of being typical of the human lineage. Indeed, Diester and Nieder (2007) have shown that by training monkeys, prefrontal neurons may acquire selectivity for abstract symbols that have been associated with visual quantities through training. After training, prefrontal neurons exhibit selectivity for a given numerosity and for the symbol associated with it by training. In their study, Diester and Nieder (2007) found very few parietal neurons with this combined selectivity. It is, however, possible that with training at an earlier age, such parietal neurons may be observed in the monkey parietal cortex. Therefore, we should consider the possibility that the first step in abstracting numerosity is shared with nonhuman primates. The second step in the abstraction process, generalization across different types of ordered sequences (Fias et al. 2007), remains more likely a typically human achievement, although here also it is difficult to assess which of our ancestors possessed this capacity.

When discussing changes in the parietal lobe during the evolution of our species, the authors quote our studies demonstrating that functional properties of parietal regions have changed during evolution (Orban et al. 2006; Vanduffel et al. 2002). In particular, we have shown that sensitivity to motion and to three-dimensional shape extracted from motion is stronger in the human than in the monkey parietal cortex. In those studies, we suggested that some of the functional differences in the parietal lobe may be related to tool use, which is much more developed among humans than in nonhuman primates. Recently, we provided direct evidence for a parietal region involved in understanding tool use that is present in humans but not monkeys (Peeters et al. 2009). Tools have the advantage that their development can be traced in the archeological record. Using this record, we speculated that this parietal area was perhaps present in *Homo erectus*, to whom the Acheulian in-

in the abstraction process (or higher-level abstraction) may be unique to modern humans. Finally, our extension of the dual systems of numerosity as a tentative foundation for humans' intuitive penchant for analogies and metaphors not only remained unscathed in the commentaries but untouched; we look forward to future dialogue on this part of our argument, as a recent book (e.g., Geary 2011) has highlighted the ubiquitousness of metaphors and their centrality to modern thinking. As Geary provocatively yet cryptically noted in his foreword, "Metaphor is a way of thought long before it is a way with words" (Geary 2011:3), which is completely consonant with our central thesis.

—Frederick L. Coolidge and Karenleigh A. Overmann

References Cited

- Ambrose, S. H. 2001. Paleolithic technology and human evolution. *Science* 291(5509):1748–1753. [GAO]
- Andres, M., S. Di Luca, and M. Pesenti. 2008. Finger counting: the missing tool? *Behavioral and Brain Sciences* 31:642–643.
- Ansari, D. 2008. Effects of development and enculturation on number representation in the brain. *Nature Reviews Neurosciences* 9:278–291.
- Ansari, D., N. Garcia, E. Lucas, K. Hamon, and B. Dhital. 2005. Neural correlates of symbolic number processing in children and adults. *Neuroreport* 16:1769–1773.
- Ardila, A. 2010. On the evolution of calculation abilities. *Frontiers in Evolutionary Neuroscience* 2(7):1–7.
- . 2011. There are two different language systems in the brain. *Journal of Behavioral and Brain Science* 1:23–36. [AA]
- Ardila, A., L. M. Galeano, and M. Rosselli. 1998. Toward a model of neuropsychological activity. *Neuropsychology Review* 8:177–189. [AA]
- Ardila, A., and M. Rosselli. 2002. Acalculia and dyscalculia. *Neuropsychology Review* 12:176–232. [AA]
- Baddeley, A. 2007. *Working memory, thought, and action*. Oxford: Oxford University Press.
- Barth, H., K. La Mont, J. Lipton, S. Dehaene, N. Kanwisher, and E. Spelke. 2006. Non-symbolic arithmetic in adults and young children. *Cognition* 98:199–222.
- Biro, D., and T. Matsuzawa. 2001. Chimpanzee numerical competence: cardinal and ordinal skills. In *Primate origins of human cognition and behavior*. T. Matsuzawa, ed. Pp. 199–225. Tokyo: Springer. [LM]
- Blum, D. 1994. *The monkey wars*. Oxford: Oxford University Press.
- Bongard, S., and A. Nieder. 2010. Basic mathematical rules are encoded by primate prefrontal cortex neurons. *Proceedings of the National Academy of Sciences of the USA* 107:2277–2282. [AN]
- Botha, R. 2008. Prehistoric shell beads as a window on language evolution. *Language and Communication* 28:197–212.
- Brannon, E. M. 2005. The independence of language and mathematical reasoning. *Proceedings of the National Academy of Sciences of the USA* 102:3177–3178.
- Bright, M. 2009. *The diversity of species*. Chicago: Heinemann.
- Bruner, E. 2004. Geometric morphometrics and paleoneurology: brain shape evolution in the genus *Homo*. *Journal of Human Evolution* 47:279–303.
- . 2010. Morphological differences in the parietal lobes within the human genus: a neurofunctional perspective. *Current Anthropology* 51(suppl. 1):S77–S88.
- Bruner, E., J. M. De la Cuétara, and R. L. Holloway. 2011a. A bivariate approach to the variation of the parietal curvature in the genus *Homo*. *Anatomical Record* 294:1548–1556. [EB]
- Bruner, E., and R. L. Holloway. 2010. A bivariate approach to the widening of the frontal lobes in the genus *Homo*. *Journal of Human Evolution* 58:138–146.
- Bruner, E., G. Manzi, and J. L. Arsuaga. 2003. Encephalization and allometric trajectories in the genus *Homo*: evidence from the Neandertal and modern lineages. *Proceedings of the National Academy of Sciences of the USA* 100(26):15335–15340.
- Bruner, E., M. Martin-Loeches, M. Burgaleta, and R. Colom. 2011b. Midsagittal brain shape correlation with intelligence and cognitive performance. *Intelligence* 39:141–147. [EB]
- Bruner, E., M. Martin-Loeches, and R. Colom. 2010. Human midsagittal brain shape variation: patterns, allometry, and integration. *Journal of Anatomy* 216:589–599. [EB]
- Burr, D., and J. Ross. 2008. A visual sense of number. *Current Biology* 18(6):425–428. [DA]
- Cantlon, J., and E. Brannon. 2006. Shared system for ordering small and large numbers in monkeys and humans. *Psychological Science* 17:401–406.
- Cantlon, J., M. Platt, and E. Brannon. 2008. Beyond the number domain. *Trends in Cognitive Sciences* 30:1–9.
- Cantlon, J. F., E. M. Brannon, E. J. Carter, and K. A. Pelphey. 2006. Functional imaging of numerical processing in adults and four-year-old children. *PLoS Biology* 4:844–854.
- Cantlon, J. F., M. E. Libertus, P. Pinel, S. Dehaene, E. M. Brannon, and K. A. Pelphey. 2009. The neural development of an abstract concept of number. *Journal of Cognitive Neuroscience* 21:2217–2229. [AN]
- Carey, S. 2009. *The origin of concepts*. Oxford: Oxford University Press.
- Carreiras, M., M. L. Seghier, S. Baquero, A. Estévez, A. Lozano, J. T. Devlin, and C. J. Price. 2009. An anatomical signature for literacy. *Nature* 461:983–986. [HD]
- Carruthers, P. 2002. Human creativity: its evolution, its cognitive basis, and its connections with childhood pretence. *British Journal for the Philosophy of Science* 53:225–249. [HD]
- Chiappe, D. L., and P. Chiappe. 2007. The role of working memory in metaphor production and comprehension. *Journal of Memory and Language* 56:172–188.
- Cohen Kadosh, R., and V. Walsh. 2009. Numerical representation in the parietal lobes: abstract or not abstract? *Behavioral and Brain Sciences* 32:313–373.
- Coolidge, F. L., K. A. Overmann, and T. Wynn. 2011. Recursion: what is it, who has it, and how did it evolve? *Wiley Interdisciplinary Reviews: Cognitive Science* 2:547–554.
- Coolidge, F. L., and T. Wynn. 2001. Executive functions of the frontal lobes and the evolutionary ascendancy of *Homo sapiens*. *Cambridge Archaeological Journal* 11:255–260.
- . 2005. Working memory, its executive functions, and the emergence of modern thinking. *Cambridge Archaeological Journal* 15:5–26.
- Crollen, V., X. Seron, and M.-P. Noël. 2011. Is finger-counting necessary for the development of arithmetic abilities? *Frontiers in Psychology* 2:1–3.
- Culham, J. C., and N. G. Kanwisher. 2001. Neuroimaging of cognitive functions in human parietal cortex. *Current Opinion in Neurobiology* 11:157–163. [EB]
- Cummins, D. D., and R. Cummins. 1999. Biological preparedness and evolutionary explanation. *Cognition* 73:B37–B53.
- Dart, R. A. 1925. *Australopithecus africanus*: the man-ape of South Africa. *Nature* 2884:195–199. [EB]
- Deacon, T. 1997. *The symbolic species: the co-evolution of language and the human brain*. London: Norton. [AN]
- De Cruz, H. 2008. An extended mind perspective on natural number representation. *Philosophical Psychology* 21:475–490. [HD]
- De Cruz, H., and J. De Smedt. 2010. Mathematical symbols as epistemic actions. *Synthese*, doi:10.1007/s11229-010-9837-9. [HD]
- Dehaene, S. 1997. *The number sense*. New York: Oxford University Press. [LM]
- . 2007. Symbols and quantities in parietal cortex: elements of a mathematical theory of number representation and manipulation. In *Sensory-motor foundations of higher cognition: attention and performance*. P. Haggard, Y. Rossetti, and M. Kawato, eds. Pp. 527–574. Oxford: Oxford University Press.
- Dehaene, S., G. Dehaene-Lambertz, and L. Cohen. 1998. Abstract representations of numbers in the animal and human brain. *Trends in Neuroscience* 21:355–361.
- Dehaene, S., E. Spelke, P. Pinel, R. Stanescu, and S. Tsivkin. 1999. Sources of mathematical thinking: behavioral and brain-imaging evidence. *Science* 284:970–974.
- Deloche, G. 1993. Aphasia and acalculia. In *Linguistic disorders and pathologies*. G. Blanken, J. Dittmann, H. Grimm, J. C. Marshall, and C. W. Wallesch, eds. Pp. 325–332. Berlin: de Gruyter. [AA]
- De Smedt, J., and H. De Cruz. 2011. The role of material culture in human time representation: calendrical systems as extensions of mental time travel. *Adaptive Behavior* 19:63–76. [HD]
- Diester, I., and A. Nieder. 2007. Semantic associations between signs and

- numerical categories in the prefrontal cortex. *PLoS Biology* 5:e294. [AN, GAO]
- . 2008. Complementary contributions of prefrontal neuron classes in abstract numerical categorization. *Journal of Neuroscience* 28:7737–7747.
- Domahs, F., K. Moeller, S. Huber, K. Willmes, and H.-C. Nuerk. 2010. Embodied numerosity: implicit hand-based representations influence symbolic number processing across cultures. *Cognition* 116:251–266.
- Durand, J. B., R. Peeters, J. F. Norman, J. T. Todd, and G. A. Orban. 2009. Parietal regions processing visual 3D shape extracted from disparity. *Neuroimage* 46(4):1114–1126. [GAO]
- Everett, D. L. 2005. Cultural constraints on grammar and cognition in Pirahã: another look at the design features of human language. *Current Anthropology* 46:621–646.
- Falk, D. 2007. Evolution of the primate brain. In *Handbook of paleoanthropology*, vol. 2. W. Henke, I. Tattersall, and T. Hardt, eds. Pp. 1133–1162. Berlin: Springer.
- Feigenson, L., S. Dehaene, and E. Spelke. 2004. Core systems of number. *Trends in Cognitive Sciences* 8:307–314.
- Fias, W., J. Lammertyn, B. Caessens, and G. A. Orban. 2007. Processing of abstract ordinal knowledge in the horizontal segment of the intraparietal sulcus. *Journal of Neuroscience* 27:8952–8956.
- Frank, M. C., D. L. Everett, E. Fedorenko, and E. Gibson. 2008. Number as a cognitive technology: evidence from Pirahã language and cognition. *Cognition* 108:819–824. [HD]
- Geary, J. 2011. *I is an other: the secret life of metaphor and how it shapes the way we see the world*. New York: HarperCollins.
- Gelman, R., and C. R. Gallistel. 2004. Language and the origin of numerical concepts. *Science* 306:441–443. [LM]
- Geschwind, N. 1964. The development of the brain and the evolution of language. *Monograph Series on Language and Linguistics* 17:155–169.
- Geva, S., P. S. Jones, J. T. Crinion, C. J. Price, J.-C. Baron, and E. A. Warburton. 2011. The neural correlates of inner speech defined by voxel-based lesion-symptom mapping. *Brain: A Journal of Neurology* 134:3071–3082.
- Gilmore, C. K., S. E. McCarthy, and E. S. Spelke. 2010. Non-symbolic arithmetic abilities and mathematics achievement in the first year of formal schooling. *Cognition* 115:394–406.
- Grefkes, C., and G. R. Fink. 2005. The functional organization of the intraparietal sulcus in humans and monkeys. *Journal of Anatomy* 207(1):3–17. [GAO]
- Gunz, P., S. Neubauer, B. Maureille, and J. J. Hublin. 2010. Brain development after birth differs between Neanderthals and modern humans. *Current Biology* 20:R921–R922. [EB]
- Hagmann P., L. Cammoun, X. Gigandet, R. Meuli, C. J. Honey, V. J. Wedeen, and O. Sporns. 2008. Mapping the structural core of human cerebral cortex. *PLoS Biology* 6:e159.
- Harnad, S. 1990. The symbol grounding problem. *Physica D: Nonlinear Phenomena* 42:335–346.
- Haun, D. B. M., F. M. Jordan, G. Vallortigara, and N. S. Clayton. 2010. Origins of spatial, temporal and numerical cognition: insights from comparative psychology. *Trends in Cognitive Sciences* 14(12):552–560.
- Hauser, M. D., N. Chomsky, and W. T. Fitch. 2002. The faculty of language: what is it, who has it, and how did it evolve? *Science* 298:1569–1579.
- Henshilwood, C. S., F. d'Errico, M. Vanhaeren, K. van Niekerk, and Z. Jacobs. 2004. Middle Stone Age shell beads from South Africa. *Science* 304:404.
- Holloway, I. D., and D. Ansari. 2009. Mapping numerical magnitudes onto symbols: the numerical distance effect and individual differences in children's mathematics achievement. *Journal of Experimental Child Psychology* 103(1):17–29. [DA]
- Holloway, R. L. 1981. Exploring the dorsal surface of hominoid brain endocasts by stereoplotter and discriminant analysis. *Philosophical Transactions of the Royal Society B: Biological Sciences* 393:155–166. [EB]
- Hubbard, E. M., M. Piazza, P. Pinel, and S. Dehaene. 2009. Numerical and spatial intuitions: a role for posterior parietal cortex? In *Cognitive biology: evolutionary and developmental perspectives on mind, brain and behavior*. L. Tommasi, L. Nadel, and M. A. Peterson, eds. Pp. 221–246. Cambridge, MA: MIT Press.
- Hurford, J. 1987. *Language and number: the emergence of a cognitive system*. Oxford: Blackwell.
- Hutchins, E. 2005. Material anchors for conceptual blends. *Journal of Pragmatics* 37:1555–1577. [LM]
- Imbo, I., A. Vandierendonck, and W. Fias. 2011. Passive hand movements disrupt adults' counting strategies. *Frontiers in Psychology* 2:1–5.
- Jackendoff, R. 1996. How language helps us think. *Pragmatics and Cognition* 4:1–34. [HD]
- Jordan, N. C., D. Kaplan, M. N. Locuniak, and C. Ramineni. 2007. Predicting first-grade math achievement from developmental number sense trajectories. *Learning Disabilities Research and Practice* 22:36–46.
- Jung, R. E., and R. J. Haier. 2007. The parieto-frontal integration theory (P-FIT) of intelligence: converging neuroimaging evidence. *Behavioural and Brain Sciences* 30:135–187. [EB]
- Kaufman, E. L., M. W. Lord, T. W. Reese, and J. Volkman. 1949. The discrimination of visual number. *American Journal of Psychology* 62:498–525.
- Kaufmann, L., F. Koppelstaetter, C. Siedentopf, I. Haala, E. Haberlandt, L. B. Zimmerhackl, S. Felber, and A. Ischebeck. 2006. Neural correlates of the number-size interference task in children. *Neuroreport* 17:587–591. [AN]
- Kirsh, D. 1995. The intelligent use of space. *Artificial Intelligence* 73:31–68. [LM]
- Klein, E., K. Moeller, K. Willmes, H.-C. Nuerk, and F. Domahs. 2011. The influence of implicit hand-based representations on mental arithmetic. *Frontiers in Psychology* 2:1–7.
- Lakoff, G., and M. Johnson. 1999. *Philosophy in the flesh: the embodied mind and its challenge to Western philosophy*. New York: Basic.
- Lakoff, G., and R. E. Núñez. 2000. *Where mathematics comes from: how the embodied mind brings mathematics into being*. New York: Basic.
- Le Corre, M., and S. Carey. 2007. One, two, three, four, nothing more: an investigation of the conceptual sources of the verbal counting principles. *Cognition* 105(2):395–438. [DA]
- Libertus, M. E., L. Feigenson, and J. Halberda. 2011. Preschool acuity of the approximate number system correlates with school math ability. *Developmental Science* 14:1292–1300.
- Lurito, J. T., D. A. Kareken, M. J. Lowe, S. H. A. Chen, and V. P. Mathews. 2000. Comparison of rhyming and word generation with fMRI. *Human Brain Mapping* 10:99–106.
- Malafouris, L. 2008. Beads for a plastic mind: the “blind man's stick” (BMS) hypothesis and the active nature of material culture. *Cambridge Archaeological Journal* 18:401–414. [LM]
- . 2010a. The brain-artefact interface (BAI): a challenge for archaeology and cultural neuroscience. *Social Cognitive and Affective Neuroscience* 5(2/3):264–273, doi:10.1093/scan/nsp057. [LM]
- . 2010b. Grasping the concept of number: how did the sapient mind move beyond approximation? In *The archaeology of measurement: comprehending heaven, earth and time in ancient societies*. C. Renfrew and I. Morley, eds. Pp. 35–42. Cambridge: Cambridge University Press.
- Maloney, E. A., E. F. Risko, F. Preston, D. Ansari, and J. Fugelsang. 2010. Challenging the reliability and validity of cognitive measures: the case of the numerical distance effect. *Acta Psychologica* 134(2):154–161. [DA]
- Mantovan, M. C., M. Delazer, M. Ermani, and G. Denes. 1999. The breakdown of calculation procedures in Alzheimer's disease. *Cortex* 35:21–38. [AA]
- Mazzocco, M. M., L. Feigenson, and J. Halberda. 2011. Impaired acuity of the approximate number system underlies mathematical learning disability (dyscalculia). *Child Development* 82:1224–1237.
- McGuire, P. K., D. A. Silbersweig, R. M. Murray, A. S. David, R. S. J. Frackowiak, and C. D. Frith. 1996. Functional anatomy of inner speech and auditory verbal imagery. *Psychological Medicine* 26:38–39. [AA]
- Menninger, K. 1992. *Number words and number symbols: a cultural history of numbers*. P. Broneer, trans. New York: Dover.
- Miller, E. K., A. Nieder, D. J. Freedman, and J. D. Wallis. 2003. Neural correlates of categories and concepts. *Current Opinion in Neurobiology* 13: 198–203.
- Mundy, E., and C. K. Gilmore. 2009. Children's mapping between symbolic and nonsymbolic representations of number. *Journal of Experimental Child Psychology* 103:490–502.
- Nieder, A. 2009. Prefrontal cortex and the evolution of symbolic reference. *Current Opinion in Neurobiology* 19:99–108. [AN]
- Nieder, A., and S. Dehaene. 2009. Representation of number in the brain. *Annual Review of Neuroscience* 32:185–208. [DA]
- Nieder, A., I. Diester, and O. Tudusciuc. 2006. Temporal and spatial enumeration processes in the primate parietal cortex. *Science* 313:1431–1435. [AN]
- Nieder, A., and E. K. Miller. 2004. A parieto-frontal network for visual numerical information in the monkey. *Proceedings of the National Academy of Sciences of the USA*. 101:7457–7462.
- Orban, G. A. 2011. The extraction of 3D shape in the visual system of human and nonhuman primates. *Annual Review of Neuroscience* 34:361–388.
- Orban, G. A., K. Claeys, K. Nelissen, R. Smans, S. Sunaert, J. T. Todd, C.

- Wardak, J. B. Durand, and W. Vanduffel. 2006. Mapping the parietal cortex of human and non-human primates. *Neuropsychologia* 44:2647–2667.
- Overmann, K., T. Wynn, and F. L. Coolidge. 2011. The prehistory of number concept. *Behavioral and Brain Sciences* 34:142–144. [LM]
- Owen, W. J., R. Borowsky, and G. E. Sarty. 2004. fMRI of two measures of phonological processing in visual word recognition: ecological validity matters. *Brain and Language* 90:40–46.
- Patel, A. D. 2008. *Music, language, and the brain*. New York: Oxford University Press. [HD]
- Peeters, R., L. Simone, K. Nelissen, M. Fabbri-Destro, W. Vanduffel, G. Rizzolatti, and G. A. Orban. 2009. The representation of tool use in humans and monkeys: common and uniquely human features. *Journal of Neuroscience* 29(37):11523–11539. [GAO]
- Peirce, C. 1955. *Philosophical writings of Peirce*. J. Buchler, ed. New York: Dover. [AN]
- Penn, D. C., K. J. Holyoak, and D. J. Povineli. 2008. Darwin's mistake: explaining the discontinuity between human and nonhuman minds. *Behavioral and Brain Sciences* 31:109–178. [HD]
- Piazza, M. 2010. Neurocognitive start-up tools for symbolic number representations. *Trends in Cognitive Sciences* 14(12):542–551.
- Piazza, M., and V. Izard. 2009. How humans count: numerosity and the parietal cortex. *Neuroscientist* 15(3):261–273. [LM]
- Ramachandran, V. S. 2004. *A brief tour of human consciousness: from impostor poodles to purple numbers*. New York: Pi.
- Reuland, E. 2010. Imagination, planning, and working memory: the emergence of language. *Current Anthropology* 51(suppl. 1):S99–S110.
- Rips, L. J., A. Bloomfield, and J. Asmuth. 2008. From numerical concepts to concepts of number. *Behavioral and Brain Sciences* 31:623–642.
- Rivera, S. M., A. L. Reiss, M. A. Eckert, and V. Menon. 2005. Developmental changes in mental arithmetic: evidence for increased functional specialization in the left inferior parietal cortex. *Cerebral Cortex* 15:1779–1790. [AN]
- Roggeman, C., S. Santens, W. Fias, and T. Verguts. 2011. Stages of nonsymbolic number processing in occipitoparietal cortex disentangled by fMRI adaptation. *Journal of Neuroscience* 31(19):7168–7173. [DA]
- Roux, F. E., S. Boetto, O. Sacko, F. Chollet, and M. Trémoulet. 2003. Writing, calculating, and finger recognition in the region of the angular gyrus: a cortical stimulation study of Gerstmann syndrome. *Journal of Neurosurgery* 99:716–727.
- Santens, S., C. Roggeman, W. Fias, and T. Verguts. 2009. Number processing pathways in human parietal cortex. *Cerebral Cortex* 20(1):77–88. [DA]
- Sato, M., L. Cattaneo, G. Rizzolatti, and V. Gallese. 2007. Numbers within our hands: modulation of corticospinal excitability of hand muscles during numerical judgment. *Journal of Cognitive Neuroscience* 19:684–693.
- Sawamura, H., G. A. Orban, and R. Vogels. 2006. Selectivity of neuronal adaptation does not match response selectivity: a single-cell study of the fMRI adaptation paradigm. *Neuron* 49(2):307–318. [GAO]
- Smith, N. 2004. *Chomsky: ideas and ideals*. 2nd edition. Cambridge: Cambridge University Press.
- Sterelny, K. 2010. Minds: extended or scaffolded? *Phenomenology and the Cognitive Sciences* 9:465–481. [HD]
- Tang, Y., W. Zhang, K. Chen, S. Feng, Y. Ji, J. Shen, E. Reiman, and Y. Liu. 2006. Arithmetic processing in the brain shaped by cultures. *Proceedings of the National Academy of Sciences of the USA* 103:10775–10780. [HD]
- Tattersall, I. 2009. Language and the origin of symbolic thought. In *Cognitive archaeology and human evolution*. S. de Beaune, F. L. Coolidge, and T. Wynn, eds. Pp. 109–116. Cambridge: Cambridge University Press.
- Tobias, P. V. 1987. The brain of *Homo habilis*: a new level of organization in cerebral evolution. *Journal of Human Evolution* 16:741–761. [EB]
- Tomasello, M., and M. Carpenter. 2007. Shared intentionality. *Developmental Science* 10:121–125. [HD]
- Trinkhaus, E. 1995. Neanderthal mortality patterns. *Journal of Archaeological Science* 22:121–142.
- Vanduffel, W., D. Fize, H. Peuskens, K. Denys, S. Sunaert, J. T. Todd, and G. A. Orban. 2002. Extracting 3D from motion: differences in human and monkey intraparietal cortex. *Science* 298(5592):413–415. [GAO]
- Van Essen, D. C., and D. L. Dierker. 2007. Surface-based and probabilistic atlases of primate cerebral cortex. *Neuron* 56(2):209–225. [GAO]
- VanMarle, K., and K. Wynn. 2010. Tracking and quantifying objects and non-cohesive substances. *Developmental Science*, doi:10.1111/j.1467-7687.2010.00998.
- Vygotsky, L. S. 1962. *Thought and language*. Cambridge, MA: MIT Press. [AA]
- Wadley, L., T. Hodgskiss, and M. Grant. 2009. Implications for complex cognition from the hafting of tools with compound adhesives in the Middle Stone Age, South Africa. *Proceedings of the National Academy of Sciences of the USA* 106:9590–9594.
- Wagner, J. B., and S. C. Johnson. 2011. An association between understanding cardinality and analog magnitude representations in preschoolers. *Cognition* 119(1):10–22. [DA]
- Weidenreich, F. 1936. Observations on the form and proportions of the endocranial casts of *Sinanthropus pekinensis*, other hominids and the great apes: a comparative study of brain size. *Palaeontologia Sinica*, ser. D, 3:1–50. [EB]
- Whitehead, A. N. 1911. *An introduction to mathematics*. New York: Holt.
- Wiese, H. 2003. Iconic and non-iconic stages in number development: the role of language. *Trends in Cognitive Sciences* 7:385–390. [AN]
- Wynn, T. 2009. Hafted spears and the archeology of cognition. *Proceedings of the National Academy of Sciences of the USA* 106:9544–9545.
- Wynn, T., and F. L. Coolidge. 2005. The effect of enhanced working memory on language. *Journal of Human Evolution* 50:230–231.
- . 2012. *How to think like a Neanderthal*. Oxford: Oxford University Press.
- Zamarian, L., A. Ischebeck, and M. Delazer. 2009. Neuroscience of learning arithmetic: evidence from brain imaging studies. *Neuroscience and Biobehavioral Reviews* 33:909–925.
- Zilhão, J., D. E. Angelucci, E. Badal-García, F. d'Errico, F. Daniel, L. Dayet, K. Douka, et al. 2010. Symbolic use of marine shells and mineral pigments by Iberian Neanderthals. *Proceedings of the National Academy of Sciences of the USA* 107:1023–1028.